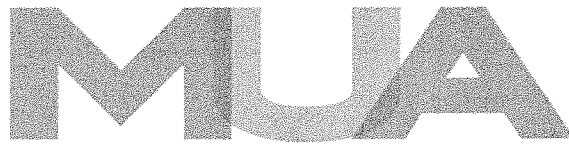


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**UNDERGRADUATE UNIVERSITY EXAMINATIONS**

**SCHOOL OF MANAGEMENT AND LEADERSHIP**

**DEGREE OF BACHELOR OF MANAGEMENT AND LEADERSHIP**

**BML 301 : FINANCIAL MANAGEMENT**

**DATE: 16<sup>TH</sup> DECEMBER 2016**

**DURATION: 2 HOURS**

**MAXIMUM MARKS: 70**

**INSTRUCTIONS:**

1. Write your registration number on the answer booklet.
2. **DO NOT** write on this question paper.
3. This paper contains **SIX (6)** questions.
4. Question **ONE** is compulsory.
5. Answer any other **THREE** questions.
6. Question **ONE** carries **25 MARKS** and the rest carry **15 MARKS** each.
7. Write all your answers in the Examination answer booklet provided.

**QUESTION ONE**

- a) Discuss the goals of a firm, giving relevant examples in each case (10 marks)
- b) There exists a number of conflicts between various stakeholders in a firm. Identify and briefly explain the TWO main forms of agency relationship in a firm and solutions to these conflicts: (10 marks)
- c) Discuss the Efficient Market Hypothesis (5 marks)

**QUESTION TWO**

Alex wishes to determine the future value at the end of two years of a Kshs 150,000 deposit made today into an account paying a nominal interest rate of 12%

- a) Find the future value of Alex's deposit assuming that interest rate is compounded:
  - i) Annually
  - ii) Quarterly
  - iii) Monthly (9 marks)
- b) Using your answer in (a) demonstrate the relationship between compounding frequency and future value (3 marks)
- c) Differentiate between an ordinary annuity, an annuity due and a perpetuity in reference to time value of money (3 marks)

**QUESTION THREE**

FirstRand Limited presented the following financial statements on 30 June 2016.

**Income statement for the year ended 30 June 2016**

	KShs.
Sales (all on credit)	<u>4,000,000</u>
Operating profit	440,000
Less: debenture interest	<u>40,000</u>
	400,000
Corporation tax	<u>176,000</u>
	224,000
Ordinary dividends proposed	<u>107,200</u>
Retained profit	<u>116,800</u>

**Balance Sheet as at 30 June 2016**

	KShs.	KShs.	KShs.
<b>Fixed assets:</b>			
Freehold property (Net book value)			480,000
Plant and machinery (Net book value)			800,000
Motor vehicle (Net book value)			200,000
Furniture and fittings			<u>200,000</u>
			1,680,000
<b>Current assets:</b>			
Stock		1,000,000	
Debtors		400,000	
Investments		<u>120,000</u>	
		1,520,000	
<b>Current liabilities</b>			
Trade creditors	238,400		
Bank overdraft	878,400		
Corporation tax	176,000		
Dividend payable	<u>107,200</u>	<u>(1,400,000)</u>	<u>120,000</u>
			1,800,000
<b>Financed by:</b>			
Authorized share capital: 800,000 Sh.1 ordinary shares			400,000
Issued and fully paid: 400,000 Sh.1 Ordinary shares			200,000
Capital reserve			800,000
Revenue reserve			<u>400,000</u>
			<u>1,800,000</u>

**Additional information:**

1. The purchases for the year were KShs 2,160,000 while the cost of sales was KShs 3,000,000.
2. The market price of the company's shares as at 30 June 2016 was Sh.5.

**Required:**

(a) Compute the following ratios for FirstRand Limited:

- |       |                                      |           |
|-------|--------------------------------------|-----------|
| (i)   | Return on capital employed           | (2 marks) |
| (ii)  | Turnover of capital                  | (2 marks) |
| (iii) | Operating expenses ratio.            | (2 marks) |
| (iv)  | Accounts receivable turnover in days | (2 marks) |
| (v)   | Dividend yield.                      | (2 marks) |
| (vi)  | Price earnings ratio                 | (2 marks) |
| (vii) | Current ratio                        | (3 marks) |

**QUESTION FOUR**

- (a) "Since debt capital is cheaper than equity, companies should resort to one hundred percent use of debt to finance their investments".

Discuss the limitations of the above financing policy. (5 marks)

- (b) The capital structure of Sabina Ltd on book values is as shown below;

Source of finance	Amounts (Kshs)
Ordinary share capital @Kshs10	400,000
Retained earnings	200,000
10% Preference shares @Kshs 20	100,000
12% Debentures Kshs 100	<u>200,000</u>
	900,000

**Additional information:**

- Currently the firm has been paying dividend per share of Sh.5. The DPS is expected to grow at 5% p.a. in future. The current MPS is Sh.40.
- The current market price of a debenture is Kshs 90
- Preference shares were issued 10 years ago and are still trading at par value
- Tax rate is 30%

**Required**

- Calculate the component cost of each source of capital (8 marks)
- Calculate the Weighted average cost of capital (WACC) (2 marks)

**QUESTION FIVE**

- Adequate working capital is essential for the efficient operation of a firm. Various factors influence the level of working capital. List and briefly explain any THREE determinants of working capital (6 marks)
- Given that the annual demand for materials is 5,000 tonnes. The ordering cost per order is Kshs 1,200, cost per unit is Kshs 50 and the carrying cost is estimated at Kshs 240 per annum. Compute the economic order quantity (4 marks)
- Explain any FIVE objectives of inventory control (5 marks)

**QUESTION SIX**

- a) Identify and explain any SIX sources of funds that are available to investors in case they want to expand their business. (6 marks)
- b) Brainwise construction limited invested Kshs 2,000,000 in project X at the beginning of year and received of Kshs 400,000, Kshs 800,000, Kshs 500,000, Kshs 400,000 and Kshs 300,000 at the end of year 1 to 5 respectively. The company's required rate of return is 9% p.a.

**Required:**

- i. Calculate the Net Present Value (NPV) of these cash flows (7 marks)
- ii. Comment, giving reasons on whether Project X was worth undertaking (2 marks)

## Present Value and Future Value Tables

Table A-1 Future Value Interest Factors for One Dollar Compounded at  $k$  Percent for  $n$  Periods:  $FVIF_{k,n} = (1 + k)^n$ 

Period	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%	11%	12%	13%	14%	15%	16%	17%	18%	19%	20%	21%	22%	23%	24%	25%	26%	27%	28%	29%	30%
1	1.0100	1.0200	1.0300	1.0400	1.0500	1.0600	1.0700	1.0800	1.0900	1.1000	1.1100	1.1200	1.1300	1.1400	1.1500	1.1600	1.1700	1.1800	1.1900	1.2000	1.2100	1.2200	1.2300	1.2400	1.2500	1.2600	1.2700	1.2800	1.2900	1.3000
2	1.0201	1.0404	1.0609	1.0816	1.1025	1.1236	1.1449	1.1664	1.1881	1.2100	1.2321	1.2544	1.2769	1.2996	1.3225	1.3456	1.3689	1.3924	1.4161	1.4399	1.4639	1.4881	1.5125	1.5371	1.5619	1.5869	1.6121	1.6375	1.6631	1.6889
3	1.0303	1.0612	1.0927	1.1248	1.1576	1.1910	1.2250	1.2597	1.2950	1.3310	1.3676	1.4049	1.4429	1.4815	1.5207	1.5605	1.6009	1.6419	1.6835	1.7257	1.7685	1.8119	1.8559	1.9005	1.9457	1.9915	2.0379	2.0849	2.1325	2.1807
4	1.0406	1.0824	1.1253	1.1693	1.2145	1.2609	1.3086	1.3576	1.4079	1.4594	1.5121	1.5661	1.6213	1.6777	1.7353	1.7941	1.8541	1.9153	1.9777	2.0413	2.1061	2.1721	2.2393	2.3077	2.3773	2.4481	2.5199	2.5929	2.6669	2.7419
5	1.0510	1.1041	1.1583	1.2137	1.2703	1.3282	1.3873	1.4476	1.5091	1.5719	1.6359	1.7011	1.7675	1.8351	1.9039	1.9739	2.0451	2.1175	2.1911	2.2659	2.3419	2.4191	2.4975	2.5771	2.6579	2.7399	2.8231	2.9075	2.9931	3.0799
6	1.0613	1.1262	1.1923	1.2597	1.3285	1.3987	1.4703	1.5433	1.6177	1.6935	1.7707	1.8493	1.9293	2.0107	2.0935	2.1777	2.2633	2.3503	2.4387	2.5285	2.6197	2.7123	2.8063	2.9017	2.9985	3.0967	3.1963	3.2973	3.3997	3.5035
7	1.0721	1.1487	1.2269	1.3067	1.3881	1.4711	1.5557	1.6419	1.7297	1.8191	1.9101	1.9927	2.0869	2.1827	2.2799	2.3785	2.4785	2.5799	2.6827	2.7869	2.8925	2.9995	3.1079	3.2177	3.3289	3.4415	3.5555	3.6709	3.7877	3.9059
8	1.0829	1.1717	1.2627	1.3559	1.4513	1.5489	1.6487	1.7507	1.8549	1.9613	2.0699	2.1807	2.2937	2.4089	2.5263	2.6459	2.7677	2.8917	3.0179	3.1463	3.2769	3.4097	3.5447	3.6819	3.8213	3.9629	4.1067	4.2527	4.4009	4.5513
9	1.0937	1.1951	1.3007	1.4095	1.5217	1.6373	1.7563	1.8787	1.9945	2.1137	2.2363	2.3623	2.4917	2.6245	2.7607	2.9003	3.0433	3.1897	3.3395	3.4927	3.6493	3.8093	3.9727	4.1395	4.3097	4.4833	4.6595	4.8383	5.0197	5.2037
10	1.1046	1.2190	1.3397	1.4657	1.5969	1.7333	1.8750	2.0221	2.1745	2.3323	2.4955	2.6641	2.8381	3.0175	3.2023	3.3925	3.5881	3.7891	3.9955	4.2073	4.4245	4.6471	4.8751	5.1085	5.3473	5.5915	5.8411	6.0961	6.3565	6.6223
11	1.1157	1.2434	1.3767	1.5157	1.6603	1.8105	1.9664	2.1281	2.2955	2.4687	2.6477	2.8325	3.0231	3.2195	3.4217	3.6297	3.8435	4.0631	4.2885	4.5197	4.7567	4.9995	5.2481	5.4925	5.7427	5.9987	6.2605	6.5281	6.7915	7.0607
12	1.1268	1.2682	1.4167	1.5713	1.7321	1.8991	2.0723	2.2517	2.4373	2.6291	2.8269	3.0307	3.2405	3.4563	3.6781	3.9059	4.1397	4.3795	4.6253	4.8771	5.1349	5.3987	5.6685	5.9443	6.2261	6.5139	6.8077	7.1075	7.4133	7.7251
13	1.1381	1.2936	1.4557	1.6243	1.7995	1.9813	2.1697	2.3647	2.5663	2.7745	2.9893	3.2107	3.4387	3.6731	3.9139	4.1611	4.4147	4.6747	4.9411	5.2139	5.4931	5.7787	6.0707	6.3691	6.6739	6.9851	7.3027	7.6267	7.9571	8.2939
14	1.1495	1.3195	1.5007	1.6893	1.8855	2.0893	2.2997	2.5167	2.7403	2.9705	3.2073	3.4507	3.7007	3.9573	4.2205	4.4895	4.7643	5.0451	5.3319	5.6247	5.9235	6.2283	6.5391	6.8559	7.1787	7.5075	7.8423	8.1831	8.5301	8.8833
15	1.1610	1.3459	1.5383	1.7403	1.9509	2.1693	2.3955	2.6297	2.8719	3.1221	3.3803	3.6465	3.9207	4.2029	4.4931	4.7913	5.0965	5.4087	5.7279	6.0541	6.3873	6.7275	7.0747	7.4289	7.7901	8.1583	8.5335	8.9157	9.3039	9.6981
16	1.1726	1.3728	1.5767	1.7903	2.0125	2.2433	2.4827	2.7307	2.9873	3.2525	3.5263	3.8087	4.0997	4.3993	4.7075	5.0243	5.3487	5.6807	6.0193	6.3645	6.7163	7.0745	7.4391	7.8101	8.1875	8.5713	8.9615	9.3581	9.7611	10.1705
17	1.1843	1.4002	1.6157	1.8403	2.0741	2.3173	2.5697	2.8313	3.0921	3.3621	3.6413	3.9297	4.2273	4.5341	4.8491	5.1723	5.5037	5.8433	6.1911	6.5471	6.9113	7.2837	7.6643	8.0531	8.4501	8.8553	9.2687	9.6903	10.1201	10.5581
18	1.1961	1.4282	1.6567	1.8953	2.1441	2.3933	2.6527	2.9213	3.1991	3.4861	3.7823	4.0877	4.3923	4.7061	5.0291	5.3613	5.7027	6.0533	6.4131	6.7813	7.1579	7.5429	7.9363	8.3381	8.7483	9.1669	9.5939	10.0293	10.4731	10.9253
19	1.2081	1.4568	1.7007	1.9543	2.2185	2.4833	2.7587	3.0447	3.3413	3.6485	3.9663	4.2947	4.6327	4.9803	5.3375	5.7043	6.0807	6.4667	6.8613	7.2645	7.6763	8.0967	8.5257	8.9633	9.4095	9.8643	10.3277	10.7997	11.2793	11.7665
20	1.2202	1.4859	1.8001	2.1113	2.4333	2.7663	3.1103	3.4653	3.8313	4.2083	4.5963	4.9953	5.4053	5.8263	6.2583	6.7013	7.1553	7.6203	8.0963	8.5833	9.0813	9.5903	10.1113	10.6443	11.1893	11.7463	12.3153	12.8963	13.4893	14.0943
21	1.2324	1.5157	1.8503	2.2287	2.5723	2.9273	3.2937	3.6717	4.0613	4.4623	4.8747	5.2983	5.7333	6.1797	6.6373	7.1063	7.5867	8.0787	8.5823	9.0973	9.6237	10.1613	10.7103	11.2703	11.8423	12.4263	13.0223	13.6303	14.2503	14.8823
22	1.2447	1.5400	1.9101	2.3093	2.6743	3.0503	3.4373	3.8353	4.2443	4.6643	5.0953	5.5373	5.9903	6.4543	6.9293	7.4153	7.9123	8.4203	8.9393	9.4693	10.0103	10.5623	11.1253	11.7003	12.2873	12.8863	13.4973	14.1203	14.7553	15.4023
23	1.2572	1.5709	1.9507	2.3647	2.7503	3.1473	3.5553	3.9743	4.4043	4.8453	5.2973	5.7603	6.2343	6.7193	7.2153	7.7223	8.2403	8.7693	9.3093	9.8603	10.4223	10.9953	11.5793	12.1743	12.7813	13.3993	14.0283	14.6683	15.3193	15.9813
24	1.2697	1.6004	2.0028	2.4283	2.8353	3.2533	3.6823	4.1223	4.5733	5.0353	5.5083	5.9923	6.4873	6.9933	7.5103	8.0383	8.5773	9.1273	9.6883	10.2603	10.8433	11.4373	12.0423	12.6583	13.2853	13.9233	14.5723	15.2323	15.9033	16.5853
25	1.2824	1.6400	2.0938	2.5403	2.9673	3.4053	3.8543	4.3143	4.7853	5.2673	5.7603	6.2643	6.7793	7.3053	7.8423	8.3903	8.9493	9.5193	10.0993	10.6903	11.2923	11.9053	12.5293	13.1643	13.8103	14.4673	15.1353	15.8143	16.5043	17.2053
26	1.2952	1.6800	2.1903	2.6583	3.1053	3.5633	4.0323	4.5123	4.9933	5.4853	5.9883	6.5023	7.0273	7.5633	8.1103	8.6683	9.2373	9.8173	10.4083	11.0103	11.6233	12.2473	12.8823	13.5283	14.1853	14.8533	15.5323	16.2223	16.9233	17.6353
27	1.3081	1.7200	2.2913	2.7763	3.2433	3.7213	4.2103	4.7103	5.2213	5.7433	6.2763	6.8203	7.3753	7.9413	8.5183	9.1063	9.7053	10.3153	10.9363	11.5683	12.2113	12.8653	13.5303	14.2063	14.8933	15.5913	16.3003	17.0203	17.7513	18.4933
28	1.3211	1.7600	2.3973	2.8903	3.3783	3.8673	4.3673	4.8783	5.3993	5.9313	6.4743	7.0283	7.5933	8.1693	8.7563	9.3543	9.9633	10.5833	11.2143	11.8563	12.5093	13.1733	13.8483	14.5343	15.2313	15.9393	16.6583	17.3883	18.1293	18.8813
29	1.3342	1.8000	2.5003	3.0053	3.4953	3.9953	4.5053	5.0263	5.5573	6.0983	6.6503	7.2133	7.7873	8.3623	8.9483	9.5453	10.1533	10.7723	11.4023	12.0433	12.6953	13.3583	14.0323	14.7173	15.4133	16.1203	16.8383	17.5673	18.3073	19.0583
30	1.3473	1.8400	2.6093	3.1243	3.6243	4.1343	4.6543	5.1843	5.7243	6.2743	6.8343	7.4043	7.9843	8.5743	9.1743	9.7843	10.4043	11.0343	11.6743	12.3243	12.9843	13.6543	14.3343	15.0243	15.7243	16.4343	17.1543	17.8843	18.6243	19.3743
31	1.3605	1.8800	2.7243	3.2583	3.7683	4.2883	4.8183	5.3583	5.9083	6.4683	7.0383	7.6183	8.2083	8.8083	9.4183	10.0383	10.6683	11.3083	11.9583	12.6183	13.2883	13.9683	14.6583	15.3583	16.0683	16.7883	17.5183	18.2583	18.9983	19.7483
32	1.3738	1.9200	2.8393	3.3973	3.9173	4.4473	4.9873	5.5373	6.0973	6.6673	7.2473	7.8373	8.4373	9.0473	9.6673	10.2973	10.9373	11.5873	12.2473	12.9173	13.5973	14.2873	14.9873	15.6973	16.4173	17.1473	17.8873	18.6373	19.3973	20.1673
33	1.3871	1.9600	2.9543	3.5363	4.0663	4.6063	5.1563	5.7163	6.2863	6.8663	7.4563	8.0563	8.6663	9.2863	9.9163	10.5563	11.2063	11.8663	12.5363	13.2163	13.9063	14.6063	15.3163	16.0363	16.7663	17.5063	18.2563	19.0163	19.7863	20.5663
34	1.4005	2.0000	3.0743	3.6753	4.2153	4.7653	5.3253	5.8953	6.4753	7.0653	7.6653	8.2753	8.8953	9.5253	10.1653	10.8153	11.4753	12.1453	12.8253	13.5153	14.2153	14.9253	15.6453	16.3753	17.1153	17.8653	18.6253	19.3953	20.1753	20.9653
35	1.4140	2.0400	3.1993	3.8193	4.3693	4.9293	5.4993	6.0793	6.6693	7.2693	7.8793	8.4993	9.1293	9.7693																

Table A-3 Present Value Interest Factors for One Dollar Discounted at  $k$  Percent for  $n$  Periods:  $PVIF_{k,n} = 1 / (1 + k)^n$ 

Period	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%	11%	12%	13%	14%	15%	16%	17%	18%	19%	20%	21%	22%	23%	24%	25%	26%	27%	28%	29%	30%
1	0.9901	0.9804	0.9709	0.9615	0.9524	0.9434	0.9346	0.9259	0.9174	0.9091	0.9009	0.8929	0.8850	0.8772	0.8696	0.8621	0.8548	0.8476	0.8405	0.8335	0.8266	0.8198	0.8131	0.8065	0.8000	0.7937	0.7874	0.7812	0.7751	0.7691
2	0.9803	0.9612	0.9426	0.9246	0.9070	0.8900	0.8734	0.8573	0.8417	0.8264	0.8116	0.7972	0.7831	0.7695	0.7564	0.7437	0.7312	0.7189	0.7069	0.6951	0.6835	0.6721	0.6609	0.6498	0.6389	0.6282	0.6177	0.6073	0.5971	0.5871
3	0.9706	0.9423	0.9151	0.8890	0.8638	0.8396	0.8163	0.7938	0.7722	0.7513	0.7312	0.7118	0.6931	0.6750	0.6575	0.6407	0.6245	0.6088	0.5935	0.5785	0.5638	0.5494	0.5352	0.5212	0.5075	0.4941	0.4809	0.4680	0.4553	0.4428
4	0.9610	0.9238	0.8885	0.8548	0.8227	0.7921	0.7629	0.7350	0.7084	0.6830	0.6587	0.6355	0.6133	0.5921	0.5718	0.5523	0.5332	0.5144	0.4959	0.4777	0.4598	0.4422	0.4249	0.4079	0.3912	0.3748	0.3587	0.3428	0.3271	0.3117
5	0.9515	0.9057	0.8620	0.8219	0.7835	0.7473	0.7130	0.6806	0.6499	0.6209	0.5933	0.5674	0.5428	0.5194	0.4972	0.4761	0.4561	0.4372	0.4185	0.4000	0.3827	0.3656	0.3488	0.3323	0.3161	0.2999	0.2841	0.2686	0.2533	0.2382
6	0.9420	0.8880	0.8373	0.7903	0.7462	0.7050	0.6663	0.6302	0.5963	0.5643	0.5340	0.5066	0.4803	0.4556	0.4323	0.4104	0.3899	0.3706	0.3515	0.3327	0.3141	0.2958	0.2778	0.2599	0.2423	0.2250	0.2080	0.1913	0.1749	0.1587
7	0.9327	0.8706	0.8131	0.7599	0.7107	0.6651	0.6227	0.5833	0.5470	0.5132	0.4817	0.4523	0.4251	0.3996	0.3759	0.3538	0.3331	0.3137	0.2946	0.2758	0.2573	0.2390	0.2210	0.2033	0.1859	0.1688	0.1519	0.1353	0.1190	0.1029
8	0.9235	0.8535	0.7894	0.7307	0.6768	0.6274	0.5820	0.5403	0.5019	0.4665	0.4333	0.4033	0.3762	0.3509	0.3269	0.3040	0.2823	0.2610	0.2400	0.2193	0.1989	0.1788	0.1589	0.1393	0.1199	0.1008	0.0819	0.0633	0.0449	0.0267
9	0.9143	0.8368	0.7664	0.7028	0.6446	0.5919	0.5439	0.5002	0.4604	0.4241	0.3909	0.3606	0.3329	0.3075	0.2843	0.2630	0.2420	0.2213	0.2009	0.1808	0.1609	0.1413	0.1219	0.1028	0.0839	0.0652	0.0467	0.0283	0.0100	0.0000
10	0.9053	0.8203	0.7441	0.6756	0.6139	0.5584	0.5083	0.4632	0.4224	0.3853	0.3522	0.3220	0.2946	0.2697	0.2472	0.2267	0.2065	0.1866	0.1670	0.1477	0.1286	0.1097	0.0910	0.0726	0.0544	0.0364	0.0186	0.0010	0.0000	0.0000
11	0.8963	0.8043	0.7224	0.6496	0.5847	0.5268	0.4751	0.4289	0.3875	0.3503	0.3173	0.2875	0.2607	0.2366	0.2149	0.1954	0.1761	0.1571	0.1383	0.1197	0.1013	0.0831	0.0651	0.0473	0.0297	0.0123	0.0000	0.0000	0.0000	0.0000
12	0.8874	0.7885	0.7014	0.6246	0.5568	0.4950	0.4400	0.3911	0.3475	0.3083	0.2733	0.2423	0.2151	0.1906	0.1685	0.1487	0.1301	0.1118	0.0937	0.0758	0.0581	0.0406	0.0233	0.0062	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
13	0.8787	0.7739	0.6818	0.6006	0.5303	0.4653	0.4110	0.3597	0.3192	0.2793	0.2433	0.2118	0.1843	0.1604	0.1391	0.1193	0.1008	0.0826	0.0646	0.0468	0.0292	0.0118	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
14	0.8700	0.7593	0.6611	0.5752	0.5031	0.4423	0.3878	0.3405	0.2992	0.2633	0.2312	0.2033	0.1793	0.1587	0.1401	0.1229	0.1069	0.0911	0.0755	0.0601	0.0448	0.0296	0.0145	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
15	0.8613	0.7456	0.6419	0.5533	0.4810	0.4173	0.3624	0.3122	0.2745	0.2404	0.2104	0.1843	0.1618	0.1425	0.1259	0.1113	0.0977	0.0842	0.0709	0.0577	0.0446	0.0316	0.0187	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
16	0.8528	0.7320	0.6232	0.5319	0.4581	0.3936	0.3387	0.2919	0.2519	0.2176	0.1881	0.1631	0.1415	0.1229	0.1069	0.0930	0.0801	0.0673	0.0546	0.0420	0.0295	0.0171	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
17	0.8444	0.7184	0.6050	0.5114	0.4363	0.3714	0.3166	0.2703	0.2311	0.1978	0.1696	0.1456	0.1232	0.1078	0.0929	0.0802	0.0675	0.0549	0.0424	0.0299	0.0175	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
18	0.8360	0.7060	0.5884	0.4916	0.4155	0.3503	0.2959	0.2502	0.2120	0.1799	0.1528	0.1300	0.1108	0.0946	0.0806	0.0681	0.0556	0.0431	0.0306	0.0182	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
19	0.8277	0.6936	0.5713	0.4716	0.3957	0.3305	0.2765	0.2317	0.1945	0.1633	0.1377	0.1161	0.0981	0.0829	0.0703	0.0588	0.0473	0.0358	0.0243	0.0128	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
20	0.8195	0.6790	0.5537	0.4504	0.3749	0.3100	0.2564	0.2118	0.1745	0.1448	0.1200	0.1003	0.0843	0.0706	0.0589	0.0482	0.0375	0.0268	0.0161	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
21	0.8114	0.6598	0.5315	0.4258	0.3503	0.2859	0.2324	0.1878	0.1503	0.1215	0.1000	0.0839	0.0701	0.0584	0.0486	0.0397	0.0308	0.0219	0.0130	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
22	0.8034	0.6468	0.5159	0.4080	0.3333	0.2693	0.2158	0.1712	0.1337	0.1050	0.0850	0.0698	0.0571	0.0463	0.0374	0.0285	0.0196	0.0107	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
23	0.7955	0.6342	0.5007	0.3907	0.3167	0.2533	0.2000	0.1554	0.1179	0.0892	0.0701	0.0558	0.0439	0.0340	0.0251	0.0162	0.0073	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
24	0.7876	0.6217	0.4859	0.3749	0.3015	0.2387	0.1854	0.1408	0.1033	0.0746	0.0555	0.0412	0.0313	0.0224	0.0135	0.0046	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
25	0.7798	0.6095	0.4706	0.3585	0.2859	0.2230	0.1692	0.1246	0.0871	0.0584	0.0393	0.0250	0.0151	0.0062	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
26	0.7721	0.5978	0.4559	0.3436	0.2710	0.2081	0.1543	0.1097	0.0722	0.0435	0.0244	0.0101	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
27	0.7645	0.5862	0.4413	0.3289	0.2563	0.1934	0.1396	0.0950	0.0575	0.0288	0.0097	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
28	0.7570	0.5757	0.4288	0.3164	0.2438	0.1809	0.1271	0.0825	0.0450	0.0163	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
29	0.7496	0.5653	0.4164	0.3040	0.2314	0.1685	0.1147	0.0701	0.0326	0.0039	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
30	0.7423	0.5550	0.4041	0.2917	0.2191	0.1562	0.1024	0.0578	0.0203	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000

Table A-4 Present Value Interest Factors for a One-Dollar Annuity Discounted at  $k$  Percent for  $n$  Periods:  $PVIFA_{k,n} = [1 - 1/(1 + k)^n] / k$ 

Period	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%	11%	12%	13%	14%	15%	16%	20%	24%	28%	32%
1	0.9901	0.9804	0.9709	0.9615	0.9524	0.9434	0.9346	0.9259	0.9174	0.9091	0.9009	0.8929	0.8850	0.8772	0.8696	0.8621	0.8333	0.8065	0.8000	0.7902
2	1.9704	1.9416	1.9133	1.8851	1.8574	1.8304	1.8039	1.7779	1.7523	1.7271	1.7023	1.6779	1.6538	1.6300	1.6065	1.5833	1.5278	1.4568	1.4400	1.3669
3	2.9410	2.8839	2.8286	2.7751	2.7232	2.6730	2.6243	2.5771	2.5313	2.4869	2.4437	2.4018	2.3612	2.3216	2.2832	2.2459	2.1665	1.9813	1.9520	1.8161
4	3.9020	3.8077	3.7171	3.6299	3.5460	3.4653	3.3877	3.3131	3.2415	3.1728	3.1070	3.0441	2.9840	2.9267	2.8721	2.8193	2.7287	2.5887	2.4603	2.1662
5	4.8534	4.7135	4.5797	4.4518	4.3295	4.2124	4.1002	3.9927	3.8897	3.7908	3.6959	3.6048	3.5172	3.4331	3.3522	3.2743	3.0905	2.7454	2.6893	2.4356
6	5.7955	5.6014	5.4172	5.2421	5.0757	4.9173	4.7665	4.6229	4.4859	4.3553	4.2305	4.1114	3.9973	3.8887	3.7845	3.6847	3.4253	3.0205	2.9514	2.6427
7	6.7282	6.4726	6.2303	6.0021	5.7884	5.5824	5.3833	5.1908	5.0036	4.8218	4.6452	4.4738	4.3068	4.1443	3.9867	3.8340	3.4626	3.0045	2.9243	2.6011
8	7.6517	7.3255	7.0187	6.7327	6.4662	6.2098	5.9715	5.7406	5.5148	5.2941	5.0786	4.8678	4.6619	4.4613	4.2658	4.0754	3.6372	3.1412	3.0289	2.6927
9	8.5660	8.1622	7.7801	7.4333	7.1078	6.8017	6.5152	6.2469	5.9932	5.7530	5.5271	5.3052	5.1117	4.9349	4.7616	4.5925	4.0405	3.4120	3.2505	2.9140
10	9.4713	8.9828	8.5302	8.1109	7.7217	7.3601	7.0236	6.7191	6.4177	6.1446	5.8892	5.6502	5.4262	5.2161	5.0183	4.8332	4.1923	3.6119	3.3705	3.0315
11	10.3688	9.7868	9.2526	8.7605	8.3064	7.8869	7.4987	7.1390	6.8032	6.4951	6.2065	5.9377	5.6869	5.4527	5.2337	5.0266	4.3271	3.7757	3.5064	3.1473
12	11.2355	10.5755	9.9540	9.3551	8.8853	8.4338	7.9877	7.5591	7.1607	6.8137	6.4924	6.1944	5.9176	5.6603	5.4206	5.1971	4.4392	3.8514	3.7291	3.1933
13	12.1234	11.348	10.635	9.9506	9.3936	8.8527	8.3257	7.9038	7.4809	7.1034	6.7499	6.4233	6.1218	5.8424	5.5831	5.3423	4.5327	3.9124	3.7891	3.2233
14	13.004	12.106	11.296	10.563	9.8986	9.2556	8.7455	8.2442	7.7682	7.3687	6.9819	6.6283	6.3025	6.0021	5.7245	5.4675	4.6106	3.9516	3.8241	3.2487
15	13.865	12.849	11.938	11.118	10.389	9.7122	9.1879	8.5995	8.0607	7.6081	7.1909	6.8109	6.4624	6.1422	5.8474	5.5755	4.6735	4.0013	3.8593	3.2632
16	14.7116	13.578	12.561	11.652	10.836	10.106	9.4466	8.8514	8.3126	7.8237	7.3752	6.9740	6.6039	6.2651	5.9542	5.6685	4.7296	4.0333	3.8874	3.2832
17	15.562	14.292	13.166	12.166	11.274	10.477	9.7632	9.1216	8.5436	8.0216	7.5688	7.1196	6.7291	6.3729	6.0472	5.7487	4.7746	4.0591	3.9009	3.2848
18	16.3998	14.992	13.754	12.659	11.690	10.828	10.059	9.3719	8.7536	8.2014	7.7416	7.2947	6.8939	6.4678	6.1286	5.8178	4.8821	4.0729	3.9279	3.3037
19	17.2226	15.678	14.324	13.134	12.085	11.138	10.336	9.6036	8.9501	8.3649	7.8933	7.4558	6.9380	6.5004	6.1982	5.8775	4.8433	4.0697	3.9424	3.1035
20	18.0456	16.351	14.824	13.590	12.462	11.470	10.594	9.8196	9.1285	8.5136	7.9693	7.4694	6.9248	6.4231	6.2993	5.9288	4.8696	4.1103	3.9339	3.1518
21	18.8577	17.011	15.415	14.029	12.821	11.764	10.836	10.017	9.2922	8.6487	8.0751	7.5620	7.0161	6.6870	6.3123	5.9731	4.8913	4.1212	3.9631	3.1918
22	19.660	17.628	15.937	14.451	13.163	12.042	11.061	10.201	9.4404	8.7715	8.1727	7.6446	7.1095	6.7429	6.3587	6.0113	4.9045	4.1300	3.9705	3.2220
23	20.456	18.252	16.444	14.857	13.483	12.303	11.272	10.371	9.5802	8.8832	8.2654	7.7187	7.1737	6.7895	6.3988	6.0442	4.9264	4.1571	3.9764	3.2324
24	21.242	18.914	16.936	15.247	13.799	12.550	11.469	10.529	9.7066	8.9847	8.3481	7.7843	7.2829	6.8351	6.4338	6.0726	4.9371	4.1428	3.9811	3.2372
25	22.023	19.523	17.413	15.622	14.044	12.783	11.654	10.675	9.8226	9.0770	8.4217	7.8431	7.3360	6.8729	6.4641	6.0971	4.9470	4.1474	3.9849	3.2386
26	22.798	20.174	18.044	16.163	14.478	13.067	11.945	10.946	10.071	9.2922	8.6166	8.0190	7.4923	6.9952	6.5664	6.1983	5.0000	4.1520	3.9894	3.2432
27	23.567	20.868	18.738	16.756	15.069	13.461	12.338	11.315	10.517	9.696	9.0009	8.4532	7.9065	7.3888	6.9399	6.5408	5.0000	4.1566	3.9939	3.2478
28	24.330	21.595	19.474	17.399	15.713	13.856	12.681	11.651	10.837	9.9911	9.3111	8.7438	8.1844	7.6456	7.1661	6.7335	5.0000	4.1611	3.9984	3.2524
29	25.088	22.356	20.240	18.087	16.406	14.251	13.065	12.007	11.158	10.274	9.4269	8.8938	8.3552	7.8957	7.0027	6.5600	5.0000	4.1656	3.9999	3.2570
30	25.840	23.099	20.987	18.805	16.374	14.498	13.248	11.615	10.567	9.6442	8.8542	8.2754	7.7978	7.0706	6.6166	6.2103	4.9915	4.1644	3.9984	3.2330
31	26.588	23.849	21.732	19.528	16.547	14.621	13.635	11.717	10.812	9.6765	8.8586	8.1924	7.5973	7.0790	6.6211	6.2201	4.9929	4.1659	3.9987	3.2331
32	27.333	24.595	22.475	20.251	17.193	17.19	13.856	12.332	11.925	9.7791	8.9311	8.2438	7.6344	7.1059	6.6418	6.2335	4.9966	4.1659	3.9993	3.2332
33	28.076	25.340	23.218	20.974	17.882	17.882	14.081	12.552	12.133	9.963	9.1448	8.4017	7.8045	7.6752	7.1327	6.6605	4.9995	4.1660	3.9999	3.2333

